

About this course

This is a free self-study course outline written by Saving Planets. It is not a university course, it carries no academic credit, and no school is involved.

Its scope follows the first semester of calculus-based college physics (classical mechanics), the course every engineering and physics major takes first. It is modeled on the topics and depth of open materials such as OpenStax University Physics Volume 1 and MIT OpenCourseWare 8.01SC Classical Mechanics, which we link to throughout. Those organizations do not endorse this page.

What we add: every unit is tied to real aerospace and Earth-observation work, every number on the page is re-computed by a checking script before it goes live, and every lab has a home or virtual version so anyone can do it.

Work through it in order. Each unit has goals, key ideas, equations, step-by-step examples, practice with full answers, common mistakes, flashcards and a quiz. Your progress is saved only in this browser.

How this course helps save the planet

Mechanics is the physics of launching, flying and orbiting. The same equations put Earth-observing satellites such as Landsat 9 and GRACE-FO into orbit, keep them pointed, and turn tiny changes in their motion into maps of water, ice and land.

On the ground, the same ideas size wind turbines, make cars and aircraft use less energy, and help engineers plan how to move an asteroid. Each unit ends with a short, sourced section showing how its ideas help both people and nature.

Before you start

Prerequisites

- Algebra and trigonometry: solving equations, sine, cosine and tangent, the Pythagorean theorem.
- Calculus I, at least at the same time: derivatives as rates of change and integrals as areas. This course uses dv/dt and $\int v \, dt$ from Unit 1.
- Vectors in two dimensions: components, magnitude and direction.
- SI units and scientific notation.

How to study

- Read the unit, then close it and try the worked examples yourself before checking each step.
- Draw a picture for every problem. For any force problem, draw a free-body diagram before writing an equation.
- Solve with symbols first and put numbers in at the end. Then check the units and whether the size of the answer makes sense.
- Do every practice problem on paper before opening the answer. Getting it wrong first and fixing it is how the method sticks.
- Use the PhET simulations to test your intuition: predict what will happen, then run it.
- Retake the quizzes a few days later. Spaced practice beats one long session.
- Use $g = 9.81 \text{ m/s}^2$ unless a problem says otherwise, and keep three significant figures.

Lab equipment (for the wet labs)

- Meter stick and tape measure; vernier caliper if available.
- Stopwatch (a phone works) and, ideally, a phone app or school sensor that records motion or acceleration.
- Low-friction cart and track (or a smooth board), a pulley and a set of hanging masses.
- A small ball, a ramp, carbon or plain paper for marking landing spots.
- String, a dense bob (a fishing weight works) and a protractor.
- Spreadsheet software for averages, standard deviations and graphs.

Suggested 15-week schedule

About 6 to 9 hours a week: reading, practice problems and, in lab weeks, the lab.

Week	Unit	Topics	Reading
1	Measurement, Vectors & Motion in One Dimension	Units, uncertainty, vectors; Lab A	OpenStax 1.1–1.7, 2.1–2.2
2	Measurement, Vectors & Motion in One Dimension	Velocity and acceleration as derivatives; constant acceleration; free fall	OpenStax 3.1–3.5
3	Motion in Two Dimensions: Projectiles & Circles	Projectiles, relative motion, circular motion; Lab B	OpenStax 4.1–4.5
4	Newton's Laws, Friction & Circular Dynamics	Newton's laws and free-body diagrams	OpenStax 5.1–5.7
5	Newton's Laws, Friction & Circular Dynamics	Friction, connected bodies, circular dynamics; Labs C and D	OpenStax 6.1–6.4
6	Work, Energy & Power	Work, kinetic energy, power	OpenStax 7.1–7.4
7	Work, Energy & Power	Potential energy and conservation of energy; Lab E	OpenStax 8.1–8.5

Week	Unit	Topics	Reading
8	Momentum, Collisions & Rockets	Momentum, impulse, collisions, center of mass, rockets; Lab F; midterm practice	OpenStax 9.1–9.7
9	Rotation, Torque & Angular Momentum	Rotational kinematics, moment of inertia	OpenStax 10.1–10.5
10	Rotation, Torque & Angular Momentum	Torque, rolling, angular momentum; Lab G	OpenStax 10.6–10.8, 11.1–11.3
11	Gravitation & Orbits	Newton's law of gravitation, g at altitude, satellites	OpenStax 13.1–13.4
12	Gravitation & Orbits	Kepler's laws, escape speed, orbital transfers	OpenStax 13.5–13.6
13	Oscillations & Introduction to Fluids	Simple harmonic motion, pendulums, damping, resonance; Lab H	OpenStax 15.1–15.6
14	Oscillations & Introduction to Fluids	Fluids: pressure, buoyancy, continuity, Bernoulli	OpenStax 14.1–14.6
15	Review	Review and final practice set	All units

Your progress

Tick units and labs as you finish them, and take the quizzes. Progress and quiz scores are saved only in this browser, never sent to us.

Measurement, Vectors & Motion in One Dimension

How physicists measure, how vectors describe direction, and how position, velocity and acceleration are linked by calculus.

Learning objectives

By the end of this unit you can:

- Use SI units, significant figures and a stated uncertainty for every measured value.
- Add vectors by components and find a magnitude and direction.
- Define velocity as $v = dx/dt$ and acceleration as $a = dv/dt$, and read them from graphs.
- Solve constant-acceleration problems, including free fall, with the four kinematic equations.

Key concepts

- Every measurement has an uncertainty. Report a value as best estimate $\pm$ uncertainty, with units, and round the uncertainty to one or two significant figures.
- A vector has a size and a direction. Add vectors by adding their x and y components, never their magnitudes.
- Velocity is the slope of a position–time graph; acceleration is the slope of a velocity–time graph. The area under a velocity–time graph is the displacement.
- With constant acceleration, the four kinematic equations follow from integrating $a = \text{constant}$ twice.
- Near Earth's surface, every object in free fall (no air resistance) accelerates downward at $g \approx 9.81 \text{ m/s}^2$, whatever its mass.

Key equations

$$v = \frac{dx}{dt}, \quad a = \frac{dv}{dt}$$

Velocity and acceleration as derivatives

$$v = v_0 + at$$

Velocity after time t at constant acceleration

$$x = x_0 + v_0t + \frac{1}{2}at^2$$

Position after time t at constant acceleration

$$v^2 = v_0^2 + 2a(x - x_0)$$

Speed and distance, without time

$$|A| = \sqrt{A_x^2 + A_y^2}, \quad \theta = \tan^{-1}(A_y/A_x)$$

Magnitude and direction from components

Worked examples, step by step

Example 1.1 A car starts from rest and speeds up at a steady 3.0 m/s^2 for 8.0 s . How fast is it going, and how far has it traveled?

1. Known: $v_0 = 0$, $a = 3.0 \text{ m/s}^2$, $t = 8.0 \text{ s}$.
2. $v = v_0 + at = 0 + 3.0 \times 8.0 = 24 \text{ m/s}$.
3. $x = v_0 t + \frac{1}{2}at^2 = 0 + \frac{1}{2} \times 3.0 \times 8.0^2 = 96 \text{ m}$.

Answer: 24 m/s (86 km/h) after 96 m .

Example 1.2 A ball is thrown straight up at 15 m/s . How long does it take to reach the top, and how high does it go?

1. At the top, $v = 0$. Take up as positive, so $a = -9.81 \text{ m/s}^2$.
2. Time: $0 = 15 - 9.81t$, so $t = 15 \div 9.81 = 1.53 \text{ s}$.
3. Height: $0 = 15^2 - 2 \times 9.81 \times h$, so $h = 225 \div 19.62 = 11.5 \text{ m}$.

Answer: 1.53 s to the top, 11.5 m above the release point.

Example 1.3 A hiker walks 3.0 km east and then 4.0 km north. What is her displacement?

1. Components: $x = 3.0 \text{ km}$, $y = 4.0 \text{ km}$.
2. Magnitude: $\sqrt{(3.0^2 + 4.0^2)} = \sqrt{25} = 5.0 \text{ km}$.
3. Direction: $\tan^{-1}(4.0/3.0) = 53.1^\circ$ north of east.

Answer: 5.0 km at 53.1° north of east. She walked 7.0 km , but her displacement is 5.0 km .

Practice problems

Work each on paper first, then check.

1. A car moving at 27 m/s brakes at a steady 6.0 m/s^2 . How far does it travel before stopping, and how long does it take?

Distance: $0 = 27^2 - 2 \times 6.0 \times d$, so $d = 729 \div 12 = 60.8 \text{ m}$. Time: $t = 27 \div 6.0 = 4.5 \text{ s}$.

2. A stone is dropped from rest off a 20 m bridge. Ignoring air resistance, how long until it hits the water and how fast is it going?

$t = \sqrt{(2h/g)} = \sqrt{(40 \div 9.81)} = 2.02 \text{ s}$. $v = gt = 9.81 \times 2.02 = 19.8 \text{ m/s}$.

3. The position of a drone is $x(t) = 2.0t^3 - 3.0t$ (meters, seconds). Find its velocity and acceleration at $t = 2.0 \text{ s}$.

$v = dx/dt = 6.0t^2 - 3.0 = 6.0 \times 4 - 3.0 = 21 \text{ m/s}$. $a = dv/dt = 12t = 24 \text{ m/s}^2$.

4. A low Earth orbit speed is about 7.8 km/s. Convert this to km/h.

$7.8 \text{ km/s} \times 3,600 \text{ s/h} = 28,080 \text{ km/h}$, about 28,000 km/h.

5. A solar panel measures $2.50 \pm 0.02 \text{ m}$ by $1.20 \pm 0.01 \text{ m}$. Find its area and the uncertainty.

$A = 2.50 \times 1.20 = 3.00 \text{ m}^2$. Relative uncertainties: $0.02/2.50 = 0.8\%$ and $0.01/1.20 = 0.83\%$. Combine in quadrature: $\sqrt{(0.8^2 + 0.83^2)} = 1.16\%$. $\Delta A = 0.0116 \times 3.00 = 0.035 \text{ m}^2$. $A = 3.00 \pm 0.03 \text{ m}^2$.

Common misconceptions

Myth: If the velocity is zero, the acceleration must be zero too.

Actually: At the top of its flight a thrown ball has $v = 0$ but $a = -9.81 \text{ m/s}^2$. Its velocity is still changing.

Myth: Heavier objects fall faster.

Actually: Without air resistance all objects fall with the same acceleration g . Air resistance, not weight, makes a feather fall slowly.

Myth: Distance and displacement are the same thing.

Actually: Displacement is a vector from start to finish. Walking around a running track once gives a distance of 400 m and a displacement of zero.

Flashcards

Displacement

Change in position, a vector: $\Delta x = x_{\text{final}} - x_{\text{initial}}$.

Velocity

Rate of change of position, $v = dx/dt \text{ (m/s)}$.

Acceleration

Free fall

Rate of change of velocity, $a = dv/dt$ (m/s^2).

Motion under gravity alone; $a = g \approx 9.81 \text{ m/s}^2$ downward.

Uncertainty

The range within which the true value probably lies, reported as $\pm$ with units.

Vector components

$$A_x = A \cos \theta, A_y = A \sin \theta.$$

Self-check quiz

1. The slope of a velocity–time graph gives the...

position

displacement

acceleration

jerk

acceleration. $a = dv/dt$, the slope of $v(t)$. The area under $v(t)$ is the displacement.

2. A ball thrown upward is at the very top of its path. Which is true?

$v = 0$ and $a = 0$

$v = 0$ and $a = -9.81 \text{ m/s}^2$

v is maximum

a points up

$v = 0$ and $a = -9.81 \text{ m/s}^2$. Gravity keeps pulling down the whole time, so $a = -g$ even when $v = 0$.

3. Vectors of 3 N east and 4 N north are added. The resultant is...

7 N

1 N

5 N

12 N

5 N. Perpendicular components: $\sqrt{3^2 + 4^2} = 5$ N.

4. If $x(t) = 5t^2$, the velocity at $t = 3$ s is...

15 m/s

30 m/s

45 m/s

10 m/s

30 m/s. $v = dx/dt = 10t = 30$ m/s.

Try this quiz again

How this helps save the planet

Earth-observing satellites are only useful if we know exactly where they were when each picture was taken. Their positions come from integrating velocity and acceleration over time, the same calculus as this unit, checked against GPS.

Landsat 9 orbits 705 km above Earth. Knowing its position to within meters lets scientists compare images taken years apart and measure forest loss, glacier retreat and crop health, which helps people manage land and protects habitats.

Uncertainty matters just as much: a measured change only counts if it is bigger than the uncertainty in the measurement.

On Saving Planets: [Landsat 9](#) · [Physics guide](#)

Sources: [NASA: Landsat 9](https://landsat.gsfc.nasa.gov/satellites/landsat-9/) (https://landsat.gsfc.nasa.gov/satellites/landsat-9/) · [JCGM: Guide to the expression of uncertainty](https://www.bipm.org/en/committees/jc/jcgm/publications) (https://www.bipm.org/en/committees/jc/jcgm/publications)

Free learning resources

- [OpenStax University Physics 1, 3.1 Position, Displacement and Average Velocity](https://openstax.org/books/university-physics-volume-1/pages/3-1-position-displacement-and-average-velocity) (https://openstax.org/books/university-physics-volume-1/pages/3-1-position-displacement-and-average-velocity): Free textbook section with worked examples.
- [OpenStax University Physics 1, 3.4 Motion with Constant Acceleration](https://openstax.org/books/university-physics-volume-1/pages/3-4-motion-with-constant-acceleration) (https://openstax.org/books/university-physics-volume-1/pages/3-4-motion-with-constant-acceleration): Derivations and practice problems.

- MIT OpenCourseWare 8.01SC Classical Mechanics (<https://ocw.mit.edu/courses/8-01sc-classical-mechanics-fall-2016/>): Free MIT lecture videos, notes and problem sets for the whole course.
- PhET: The Moving Man (<https://phet.colorado.edu/en/simulations/moving-man>): Link position, velocity and acceleration graphs.
- PhET: Vector Addition (<https://phet.colorado.edu/en/simulations/vector-addition>): Add vectors by components.



I finished this unit

Motion in Two Dimensions: Projectiles & Circles

Split motion into independent horizontal and vertical parts, then add circular motion, the key to every orbit.

Learning objectives

By the end of this unit you can:

- Treat horizontal and vertical motion of a projectile separately and find time of flight, range and maximum height.
- Find relative velocity by vector addition.
- Calculate centripetal acceleration and explain why it points to the center.

Key concepts

- Without air resistance, a projectile has constant horizontal velocity and constant downward acceleration g . The two directions are independent and share only time.
- On level ground the range is $R = v_0^2 \sin 2\theta / g$, largest at 45° .
- An object moving in a circle at constant speed is accelerating, because its direction changes. The acceleration $a = v^2/r$ points to the center.
- Velocities add as vectors: the velocity of a boat relative to the shore is its velocity relative to the water plus the water's velocity.

Key equations

$$x = v_0 \cos \theta t, \quad y = v_0 \sin \theta t - \frac{1}{2}gt^2$$

Projectile position

$$R = \frac{v_0^2 \sin 2\theta}{g}$$

Range on level ground

$$H = \frac{(v_0 \sin \theta)^2}{2g}$$

Maximum height

$$a_c = \frac{v^2}{r} = \omega^2 r$$

Worked examples, step by step

Example 2.1 A ball is launched at 20 m/s, 30° above level ground. Find the time of flight, range and maximum height.

1. Components: $v_x = 20 \cos 30^\circ = 17.3 \text{ m/s}$; $v_y = 20 \sin 30^\circ = 10.0 \text{ m/s}$.
2. Time of flight: $t = 2v_y/g = 20.0 \div 9.81 = 2.04 \text{ s}$.
3. Range: $R = v_x t = 17.3 \times 2.04 = 35.3 \text{ m}$.
4. Height: $H = v_y^2/2g = 100 \div 19.62 = 5.10 \text{ m}$.

Answer: 2.04 s, 35.3 m, 5.10 m.

Example 2.2 A package is thrown horizontally at 12 m/s from a 45 m cliff. Where does it land?

1. Vertical: $45 = \frac{1}{2} \times 9.81 \times t^2$, so $t = \sqrt{(90 \div 9.81)} = 3.03 \text{ s}$.
2. Horizontal: $x = 12 \times 3.03 = 36.3 \text{ m}$.

Answer: 36.3 m from the base of the cliff, after 3.03 s.

Example 2.3 A satellite circles Earth at 420 km altitude at 7.66 km/s. What is its centripetal acceleration? (Earth radius 6,371 km.)

1. Orbit radius $r = 6,371 + 420 = 6,791 \text{ km} = 6.791 \times 10^6 \text{ m}$.
2. $a = v^2/r = (7,660)^2 \div 6.791 \times 10^6 = 8.64 \text{ m/s}^2$.

Answer: 8.64 m/s², about 88% of g at the surface. That acceleration is gravity itself: the satellite is in free fall around Earth.

Practice problems

Work each on paper first, then check.

1. At what angle does a projectile go farthest on level ground, and how far does it go if launched at 20 m/s?

$$45^\circ. R = v_0^2/g = 400 \div 9.81 = 40.8 \text{ m}.$$

2. A boat heads straight across a river at 4.0 m/s relative to the water. The current flows at 3.0 m/s. Find the boat's speed relative to the shore and its direction.

$\sqrt{(4.0^2 + 3.0^2)} = 5.0 \text{ m/s}$, at $\tan^{-1}(3.0/4.0) = 36.9^\circ$ downstream of straight across.

3. A car rounds a 50 m radius curve at 15 m/s. What is its centripetal acceleration?

$$a = 15^2 \div 50 = 4.5 \text{ m/s}^2.$$

4. How fast does a point on the equator move because of Earth's rotation? (Equatorial radius 6,378 km, one turn in 86,164 s.)

$v = 2\pi r/T = 2\pi \times 6.378 \times 10^6 \div 86,164 = 465 \text{ m/s}$. Rockets launched eastward near the equator get this speed for free.

Common misconceptions

Myth: A bullet fired horizontally hits the ground later than one dropped from the same height.

Actually: Vertical motion does not depend on horizontal motion. Both hit at the same time (ignoring air resistance and Earth's curvature).

Myth: Something moving in a circle at constant speed is not accelerating.

Actually: Its velocity changes direction, so it accelerates toward the center at v^2/r .

Myth: At the top of a projectile's path its velocity is zero.

Actually: Only the vertical part is zero. The horizontal part is unchanged.

Flashcards

Projectile

An object moving under gravity alone after launch.

Range

Horizontal distance on level ground: $R = v_0^2 \sin 2\theta / g$.

Centripetal acceleration

$a = v^2/r$ toward the center of a circle.

Angular speed ω

Rate of turning in rad/s; $v = \omega r$.

Relative velocity

$v_{A \text{ rel ground}} = v_{A \text{ rel B}} + v_{B \text{ rel ground}}$.

Period T

Time for one full circle: $T = 2\pi r/v$.

Self-check quiz

1. For a projectile without air resistance, the horizontal velocity...

decreases steadily

stays constant

increases

is zero at the top

stays constant. No horizontal force means no horizontal acceleration.

2. Two launch angles give the same range on level ground. Which pair?

30° and 60°

20° and 45°

10° and 50°

45° and 90°

30° and 60°. $\sin 2\theta$ is the same for complementary angles: $\sin 60^\circ = \sin 120^\circ$.

3. If speed in a circle doubles at the same radius, centripetal acceleration...

doubles

halves

quadruples

stays the same

quadruples. $a = v^2/r$, so $2^2 = 4$ times.

4. The direction of centripetal acceleration is...

along the velocity

outward

toward the center

straight down

toward the center. It always points to the center of the circle.

Try this quiz again

How this helps save the planet

An orbit is a projectile that never lands: fired fast enough sideways, it falls toward Earth at the same rate Earth's surface curves away. That is why the satellite in Example 2.3 accelerates at v^2/r while going nowhere closer.

Launch sites take advantage of Earth's rotation. Firing eastward from near the equator adds up to about 465 m/s, which saves fuel on every launch of a weather or climate satellite.

Projectile thinking also protects people on the ground: the same equations, plus drag, are used to predict where a reentering stage or piece of debris could land.

On Saving Planets: [Projectile motion with drag calculator](#) · [Orbits guide](#)

Sources: [OpenStax University Physics 1, 4.4 Circular Motion](#) (<https://openstax.org/books/university-physics-volume-1/pages/4-4-uniform-circular-motion>) · [ESA: Space debris](#) (https://www.esa.int/Space_Safety/Space_Debris)

Free learning resources

- [OpenStax University Physics 1, 4.3 Projectile Motion](https://openstax.org/books/university-physics-volume-1/pages/4-3-projectile-motion) (<https://openstax.org/books/university-physics-volume-1/pages/4-3-projectile-motion>): Free textbook section with examples and problems.
- [OpenStax University Physics 1, 4.4 Uniform and Nonuniform Circular Motion](https://openstax.org/books/university-physics-volume-1/pages/4-4-uniform-circular-motion) (<https://openstax.org/books/university-physics-volume-1/pages/4-4-uniform-circular-motion>): Centripetal acceleration in depth.
- [PhET: Projectile Motion](https://phet.colorado.edu/en/simulations/projectile-motion) (<https://phet.colorado.edu/en/simulations/projectile-motion>): Change angle, speed and air resistance.



I finished this unit

Newton's Laws, Friction & Circular Dynamics

Forces cause acceleration. Free-body diagrams and $\Sigma F = ma$ solve almost every problem in the course.

Learning objectives

By the end of this unit you can:

- State Newton's three laws and identify action–reaction pairs.
- Draw a free-body diagram and apply $\Sigma F = ma$ along chosen axes.
- Solve incline, pulley and connected-body problems with static and kinetic friction.
- Apply Newton's second law to circular motion.

Key concepts

- First law: an object keeps its velocity unless a net force acts on it.
- Second law: $\Sigma F = ma$. Net force, not any single force, sets the acceleration.
- Third law: forces come in pairs, equal in size and opposite in direction, acting on different objects.
- Static friction can be anything up to $\mu_s N$; kinetic friction is $\mu_k N$ and opposes sliding.
- In circular motion, the net inward force is $m v^2/r$. It is supplied by real forces such as tension, friction, normal force or gravity.

Key equations

$$\Sigma F = ma,$$

Newton's second law

$$W = mg$$

Weight

$$f_s \leq \mu_s N, \quad f_k = \mu_k N$$

Static and kinetic friction

$$\Sigma F_r = \frac{mv^2}{r}$$

Second law for circular motion

Worked examples, step by step

Example 3.1 A 1,500 kg car goes from 0 to 25 m/s in 10 s. What net force acts on it?

1. $a = \Delta v / \Delta t = 25 \div 10 = 2.5 \text{ m/s}^2$.
2. $\Sigma F = ma = 1,500 \times 2.5 = 3,750 \text{ N}$.

Answer: 3,750 N forward.

Example 3.2 A 5.0 kg box slides down a 30° ramp with $\mu_k = 0.20$. Find its acceleration.

1. Axes along and perpendicular to the ramp.
2. Perpendicular: $N = mg \cos 30^\circ$.
3. Along: $ma = mg \sin 30^\circ - \mu_k mg \cos 30^\circ$.
4. $a = 9.81 \times (0.500 - 0.20 \times 0.866) = 3.21 \text{ m/s}^2$. The mass cancels.

Answer: 3.21 m/s^2 down the ramp.

Example 3.3 An Atwood machine hangs 3.0 kg and 2.0 kg over a light, frictionless pulley. Find the acceleration and the tension.

1. Heavier side moves down. For 3.0 kg: $3.0g - T = 3.0a$. For 2.0 kg: $T - 2.0g = 2.0a$.
2. Add: $1.0g = 5.0a$, so $a = 9.81 \div 5 = 1.96 \text{ m/s}^2$.
3. $T = 2.0 \times (9.81 + 1.96) = 23.5 \text{ N}$.

Answer: $a = 1.96 \text{ m/s}^2$, $T = 23.5 \text{ N}$.

Practice problems

Work each on paper first, then check.

1. A 70 kg person stands on a scale in an elevator that accelerates upward at 1.5 m/s^2 . What does the scale read?

$N - mg = ma$, so $N = 70 \times (9.81 + 1.5) = 792 \text{ N}$ (it reads as if they had a mass of 80.7 kg).

2. A 40 kg crate sits on a floor with $\mu_s = 0.50$. What horizontal push just starts it moving?

$F = \mu_s mg = 0.50 \times 40 \times 9.81 = 196 \text{ N}$.

3. A rocket of mass $5.0 \times 10^5 \text{ kg}$ has $7.6 \times 10^6 \text{ N}$ of thrust at liftoff. Find its initial acceleration.

$a = (T - mg)/m = 7.6 \times 10^6 \div 5.0 \times 10^5 - 9.81 = 15.2 - 9.81 = 5.39 \text{ m/s}^2$ upward. Its thrust-to-weight ratio is 1.55.

4. A 10 N push acts on a 2.0 kg block that pushes a 3.0 kg block on a frictionless floor. Find the acceleration and the force between the blocks.

$a = 10 \div 5.0 = 2.0 \text{ m/s}^2$. The force on the 3.0 kg block is $3.0 \times 2.0 = 6.0 \text{ N}$.

5. What is the top speed for a car on a flat 40 m radius curve if $\mu_s = 0.60$?

Friction gives the inward force: $\mu_s mg = mv^2/r$, so $v = \sqrt{(\mu_s g r)} = \sqrt{(0.60 \times 9.81 \times 40)} = 15.3 \text{ m/s}$.

Common misconceptions

Myth: A moving object needs a force to keep it moving.

Actually: Only to overcome friction or drag. In space, a probe coasts for years with its engines off.

Myth: Action and reaction cancel, so nothing can accelerate.

Actually: They act on different objects, so they never cancel on one object.

Myth: The normal force always equals mg .

Actually: Only on a level surface with no vertical acceleration. On a ramp it is $mg \cos \theta$; in an accelerating elevator it changes.

Flashcards

Newton's first law

Velocity stays constant unless a net force acts.

Newton's second law

$\Sigma F = ma$.

Newton's third law

Forces come in equal, opposite pairs on different objects.

Free-body diagram

Sketch of one object with every force acting on it.

Coefficient of friction μ

Ratio of friction force to normal force; no units.

Newton (N)

$1 \text{ N} = 1 \text{ kg} \cdot \text{m/s}^2$.

Self-check quiz

1. A spacecraft coasts with its engines off far from any planet. Its velocity...

slowly decreases

stays constant

increases

drops to zero

stays constant. No net force means no acceleration (first law).

2. A rocket pushes exhaust gas backward. What pushes the rocket forward?

The air behind it

The ground

The exhaust gas pushing back on it

Nothing; it is not pushed

The exhaust gas pushing back on it. Third law: the gas pushes the rocket with an equal and opposite force. That is why rockets work in a vacuum.

3. On a frictionless ramp at angle θ , a block accelerates at...

g

$g \cos \theta$

$g \sin \theta$

$g \tan \theta$

$g \sin \theta$. Only the component of gravity along the ramp, $mg \sin \theta$, is unbalanced.

4. What supplies the centripetal force for a car turning on a flat road?

The engine

Static friction from the road

Gravity

Centrifugal force

Static friction from the road. Static friction between tires and road points toward the center of the turn.

[Try this quiz again](#)

How this helps save the planet

Newton's third law is how every rocket works: it pushes exhaust backward and the exhaust pushes it forward. Those launches carry the satellites that monitor weather, wildfires, sea level and greenhouse gases.

Friction and drag are where much of our energy goes. Lower-friction tires and bearings, and more aerodynamic vehicles, need less force at the same speed and so less fuel or battery energy.

Thrust-to-weight is the first number engineers check on any launch vehicle: below 1, it cannot lift off.

On Saving Planets: [Thrust-to-weight calculator](#) · [Earth observation](#)

Sources: [OpenStax University Physics 1, 5.3 Newton's Second Law](https://openstax.org/books/university-physics-volume-1/pages/5-3-newtons-second-law) (<https://openstax.org/books/university-physics-volume-1/pages/5-3-newtons-second-law>) · [U.S. DOE: Vehicle Technologies Office](https://www.energy.gov/eere/vehicles/vehicle-technologies-office) (<https://www.energy.gov/eere/vehicles/vehicle-technologies-office>)

Free learning resources

- [OpenStax University Physics 1, 5.3 Newton's Second Law](https://openstax.org/books/university-physics-volume-1/pages/5-3-newtons-second-law) (<https://openstax.org/books/university-physics-volume-1/pages/5-3-newtons-second-law>): Free textbook section.
- [OpenStax University Physics 1, 6.2 Friction](https://openstax.org/books/university-physics-volume-1/pages/6-2-friction) (<https://openstax.org/books/university-physics-volume-1/pages/6-2-friction>): Static and kinetic friction with examples.
- [OpenStax University Physics 1, 6.3 Centripetal Force](https://openstax.org/books/university-physics-volume-1/pages/6-3-centripetal-force) (<https://openstax.org/books/university-physics-volume-1/pages/6-3-centripetal-force>): Banked curves and circular dynamics.
- [PhET: Forces and Motion: Basics](https://phet.colorado.edu/en/simulations/forces-and-motion-basics) (<https://phet.colorado.edu/en/simulations/forces-and-motion-basics>): Net force, friction and acceleration.
- [PhET: The Ramp](https://phet.colorado.edu/en/simulations/the-ramp) (<https://phet.colorado.edu/en/simulations/the-ramp>): Forces on an incline with friction.



I finished this unit

Work, Energy & Power

Energy is the bookkeeping that makes hard force problems easy, and the language of every power plant, battery and engine.

Learning objectives

By the end of this unit you can:

- Compute work as $W = \int \mathbf{F} \cdot d\mathbf{x}$, including for a spring.
- Use the work–energy theorem and conservation of mechanical energy.
- Account for energy lost to friction, and compute power and efficiency.
- Estimate the power in wind with $P = \frac{1}{2}\rho A v^3$.

Key concepts

- Work is force times displacement along the force: $W = Fd \cos \theta$ for a constant force.
- The net work on an object equals its change in kinetic energy.
- Gravity and springs are conservative forces: their work can be stored as potential energy and given back.
- Friction turns mechanical energy into thermal energy; total energy is still conserved.
- Power is the rate of doing work, in watts (J/s).

Key equations

$$W = \int \mathbf{F} \cdot d\mathbf{x},$$

Work by a force

$$K = \frac{1}{2}mv^2, \quad W_{\text{net}} = \Delta K$$

Kinetic energy and the work–energy theorem

$$U_g = mgh, \quad U_s = \frac{1}{2}kx^2$$

Gravitational and spring potential energy

$$K_i + U_i = K_f + U_f + E_{th}$$

Energy conservation with friction

$$P = \frac{dW}{dt} = Fv$$

Power

$$P_{wind} = \frac{1}{2}\rho Av^3$$

Power carried by wind through area A

Worked examples, step by step

Example 4.1 A 1,200 kg car moving at 20 m/s brakes with a steady 6,000 N friction force. How far does it travel?

1. $K = \frac{1}{2} \times 1,200 \times 20^2 = 240,000 \text{ J}$.
2. Friction work removes it all: $6,000 \times d = 240,000$.
3. $d = 40 \text{ m}$.

Answer: 40 m.

Example 4.2 A roller coaster starts from rest 30 m above the bottom of a dip. Ignoring friction, how fast is it at the bottom?

1. $mgh = \frac{1}{2}mv^2$, so the mass cancels.
2. $v = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 30} = 24.3 \text{ m/s}$.

Answer: 24.3 m/s, whatever the path shape.

Example 4.3 A wind turbine has 50 m blades. How much power does a 10 m/s wind carry through its swept area, and what is the most any turbine could extract?

1. $A = \pi r^2 = \pi \times 50^2 = 7,854 \text{ m}^2$.
2. $P = \frac{1}{2}\rho Av^3 = \frac{1}{2} \times 1.225 \times 7,854 \times 10^3 = 4.81 \times 10^6 \text{ W}$.
3. The Betz limit says no turbine can capture more than 16/27 (59.3%) of this: $0.593 \times 4.81 \text{ MW} = 2.85 \text{ MW}$.

Answer: The wind carries 4.81 MW; at most 2.85 MW could be captured. Real turbines get less.

Practice problems

Work each on paper first, then check.

1. A spring with $k = 200 \text{ N/m}$ is compressed 0.10 m and launches a 0.050 kg ball. How fast does the ball leave?

$$\text{Stored energy } \frac{1}{2}kx^2 = \frac{1}{2} \times 200 \times 0.01 = 1.0 \text{ J. } v = \sqrt{(2 \times 1.0 \div 0.050)} = 6.32 \text{ m/s.}$$

2. A 50 N force pulls a sled 10 m at 30° above the horizontal. How much work does it do?

$$W = Fd \cos \theta = 50 \times 10 \times 0.866 = 433 \text{ J.}$$

3. How much power does it take to lift 70 kg up 3.0 m in 2.0 s ?

$$P = mgh/t = 70 \times 9.81 \times 3.0 \div 2.0 = 1,030 \text{ W.}$$

4. A $1,500 \text{ kg}$ car brakes from 25 m/s to a stop. How much kinetic energy is removed? If regenerative braking stored 60% of it, how much would that be?

$$K = \frac{1}{2} \times 1,500 \times 25^2 = 468,750 \text{ J} \approx 469 \text{ kJ. } 60\% \text{ is } 281 \text{ kJ.}$$

5. If the wind speed falls from 10 m/s to 7 m/s , by what fraction does the wind power fall?

$$\text{Power goes as } v^3: (7/10)^3 = 0.343, \text{ so it falls to about } 34\% \text{ of the original.}$$

Common misconceptions

Myth: Carrying a heavy box across a level room at steady speed does a lot of work on it.

Actually: Gravity and your upward force are perpendicular to the motion, so they do no work on the box.

Myth: Energy is lost to friction.

Actually: It is converted to thermal energy, not destroyed. It is lost only as useful mechanical energy.

Myth: A turbine twice as big in diameter gets twice the power.

Actually: Power scales with area, so doubling the diameter gives four times the power.

Flashcards

Work

$W = Fd \cos \theta$; energy transferred by a force (J).

Kinetic energy

$$K = \frac{1}{2}mv^2.$$

Potential energy

Stored energy of position: mgh , $\frac{1}{2}kx^2$.

Work-energy theorem

$$W_{\text{net}} = \Delta K.$$

Power

Rate of energy transfer, $P = dW/dt$ (W).

Betz limit

No wind turbine can capture more than $16/27 \approx 59.3\%$ of the wind's power.

Self-check quiz

1. If a car's speed doubles, its kinetic energy...

doubles

triples

quadruples

stays the same

quadruples. $K = \frac{1}{2}mv^2$, so $2^2 = 4$.

2. The SI unit of power is the...

joule

watt

newton

kilowatt-hour

watt. $1 \text{ W} = 1 \text{ J/s}$. A kilowatt-hour is energy.

3. Wind power through a turbine scales with wind speed as...

v

v^2

v^3

$\sqrt{v}$

v^3 . Mass flow $\propto v$ and kinetic energy per kg $\propto v^2$, so $P \propto v^3$.

4. The work done by kinetic friction on a sliding block is...

positive

zero

negative

depends on mass only

negative. Friction opposes the motion, so it removes kinetic energy.

Try this quiz again

How this helps save the planet

Wind turbines turn the kinetic energy of moving air into electricity. Because wind power grows with the cube of wind speed and with the square of blade length, engineers build taller towers and longer blades, which is why offshore turbines are so large.

Electric and hybrid vehicles use regenerative braking: the motor works as a generator and turns some of the car's kinetic energy back into stored battery energy instead of heat.

Energy accounting is how engineers compare clean-energy options fairly, in joules and watts rather than claims.

On Saving Planets: [Rotor hover power calculator](#) · [Calculators](#)

Sources: [U.S. DOE: How do wind turbines work?](#) (<https://www.energy.gov/eere/wind/how-do-wind-turbines-work>) · [U.S. DOE: Electric vehicle basics](#) (<https://afdc.energy.gov/vehicles/electric-basics-ev>)

Free learning resources

- [OpenStax University Physics 1, 7.3 Work–Energy Theorem](https://openstax.org/books/university-physics-volume-1/pages/7-3-work-energy-theorem) (<https://openstax.org/books/university-physics-volume-1/pages/7-3-work-energy-theorem>): Free textbook section.
- [OpenStax University Physics 1, 8.3 Conservation of Energy](https://openstax.org/books/university-physics-volume-1/pages/8-3-conservation-of-energy) (<https://openstax.org/books/university-physics-volume-1/pages/8-3-conservation-of-energy>): Energy diagrams and examples.
- [PhET: Energy Skate Park](https://phet.colorado.edu/en/simulations/energy-skate-park) (<https://phet.colorado.edu/en/simulations/energy-skate-park>): Watch kinetic, potential and thermal energy trade off.



I finished this unit

Momentum, Collisions & Rockets

Momentum is conserved in every collision and explosion. It explains rockets, and how a spacecraft moved an asteroid.

Learning objectives

By the end of this unit you can:

- Relate impulse to change in momentum, $J = \int F dt = \Delta p$.
- Apply conservation of momentum to elastic and inelastic collisions in one dimension.
- Find the center of mass of a system.
- Use the rocket equation $\Delta v = v_e \ln(m_0/m_f)$.

Key concepts

- Momentum $p = mv$ is a vector. With no external net force, total momentum of a system stays constant.
- In an elastic collision kinetic energy is also conserved; in an inelastic one some becomes heat, sound and deformation. In a perfectly inelastic collision the objects stick together.
- A longer collision time means a smaller average force for the same change in momentum. That is how airbags and crumple zones work.
- A rocket gains speed by throwing mass backward. Its speed change depends on exhaust speed and on the ratio of starting to final mass, not on how fast the fuel burns.

Key equations

$$\underline{p} = m\underline{v}, \quad J = \int F dt = \Delta p,$$

Momentum and impulse

$$m_1 v_{1i} + m_2 v_{2i} = m_1 v_{1f} + m_2 v_{2f}$$

Conservation of momentum (1D)

$$x_{cm} = \frac{\sum m_i x_i}{\sum m_i}$$

Center of mass

$$\Delta v = v_e \ln \frac{m_0}{m_f}$$

Worked examples, step by step

Example 5.1 A 0.145 kg baseball arrives at 40 m/s and leaves the bat at 50 m/s in the opposite direction. Contact lasts 1.0 ms. Find the impulse and average force.

1. Take the outgoing direction as positive: $\Delta p = 0.145 \times (50 - (-40)) = 0.145 \times 90 = 13.1 \text{ kg}\cdot\text{m/s}$.
2. $F = \Delta p / \Delta t = 13.05 \div 0.0010 = 13,000 \text{ N}$.

Answer: Impulse 13.1 kg·m/s; average force about 13,000 N.

Example 5.2 A 1,000 kg car at 20 m/s rear-ends a stopped 1,500 kg car and they lock together. Find their speed and the kinetic energy lost.

1. Momentum: $1,000 \times 20 = 2,500 \times v$, so $v = 8.0 \text{ m/s}$.
2. K before: $\frac{1}{2} \times 1,000 \times 20^2 = 200 \text{ kJ}$. K after: $\frac{1}{2} \times 2,500 \times 8.0^2 = 80 \text{ kJ}$.
3. Lost: 120 kJ, 60% of the original.

Answer: 8.0 m/s; 120 kJ turned into deformation, heat and sound.

Example 5.3 A rocket stage has an exhaust speed of 3,000 m/s and a mass ratio $m_0/m_f = 5$. What speed change can it give, ignoring gravity and drag?

1. $\Delta v = v_e \ln(m_0/m_f) = 3,000 \times \ln 5$.
2. $\ln 5 = 1.609$, so $\Delta v = 4,830 \text{ m/s}$.

Answer: About 4.83 km/s. Reaching orbit at about 7.8 km/s needs more, which is why rockets use stages.

Practice problems

Work each on paper first, then check.

1. A 2.0 kg cart at 3.0 m/s hits a 1.0 kg cart at rest in a perfectly elastic collision. Find both final velocities.

$$v_1 = (m_1 - m_2)/(m_1 + m_2) \times 3.0 = 1.0 \text{ m/s}; v_2 = 2m_1/(m_1 + m_2) \times 3.0 = 4.0 \text{ m/s. Check: K before } 9.0 \text{ J, after } 1.0 + 8.0 = 9.0 \text{ J.}$$

2. A 4.0 kg rifle fires a 0.010 kg bullet at 400 m/s. Find the rifle's recoil speed.

$0 = 0.010 \times 400 - 4.0v$, so $v = 1.0$ m/s backward.

3. A 2.0 kg mass sits at $x = 0$ and a 3.0 kg mass at $x = 5.0$ m. Where is the center of mass?

$$x_{\text{cm}} = (2.0 \times 0 + 3.0 \times 5.0) \div 5.0 = 3.0 \text{ m.}$$

4. A stage with exhaust speed 3.5 km/s must provide $\Delta v = 9.0$ km/s on its own. What mass ratio is needed?

$m_0/m_f = e^{(9.0/3.5)} = e^{2.571} = 13.1$. Only about 7.6% of the starting mass could be anything other than propellant.

Common misconceptions

Myth: A rocket needs air to push against.

Actually: It pushes on its own exhaust. Rockets work best in a vacuum.

Myth: In an inelastic collision momentum is lost.

Actually: Momentum is conserved in every collision with no external force. Kinetic energy is what is lost.

Myth: A bigger force always means a bigger change in momentum.

Actually: Impulse is force $\times$ time. A small force over a long time can change momentum as much as a big force over a short time.

Flashcards

Momentum

$p = mv$ (kg·m/s), a vector.

Impulse

$$J = \int F \, dt = \Delta p.$$

Elastic collision

Momentum and kinetic energy both conserved.

Perfectly inelastic collision

Objects stick; maximum kinetic energy lost.

Center of mass

Mass-weighted average position of a system.

Rocket equation

$$\Delta v = v_e \ln(m_0/m_f).$$

Self-check quiz

1. Which is always conserved in a collision with no external force?

Kinetic energy

Momentum

Speed

Both kinetic energy and momentum

Momentum. Momentum always; kinetic energy only in elastic collisions.

2. Airbags reduce injury mainly by...

reducing the change in momentum

increasing the stopping time

increasing the force

reducing your mass

increasing the stopping time. Same Δp over a longer time means a smaller average force.

3. In the rocket equation, doubling the exhaust speed...

doubles Δv

quadruples Δv

halves Δv

does not change Δv

doubles Δv . Δv is directly proportional to v_e .

4. Two clay balls of equal mass and equal speed hit head-on and stick. Afterward they...

move at the original speed

are at rest

move at half speed

bounce apart

are at rest. Total momentum was zero, so it stays zero.

Try this quiz again

How this helps save the planet

On Sept. 26, 2022, NASA's DART spacecraft deliberately hit the asteroid moonlet Dimorphos. Its momentum shortened Dimorphos's 11-hour-55-minute orbit around Didymos by about 33 minutes, far more than the 73-second minimum for success, because debris thrown off the asteroid added extra push.

It was the first test of moving an asteroid by kinetic impact, a way to protect people and every other living thing on Earth from a future impact. Neither asteroid was ever a threat to Earth.

The rocket equation drives cleaner launch design too: higher exhaust speed means less propellant for the same mission.

On Saving Planets: [Planetary defense](#) · [Delta-v calculator](#)

Sources: NASA: DART mission (<https://science.nasa.gov/mission/dart/>) · NASA: Asteroid's orbit and shape changed after DART impact (<https://www.nasa.gov/missions/dart/nasa-study-asteroids-orbit-shape-changed-after-dart-impact/>)

Free learning resources

- [OpenStax University Physics 1, 9.3 Conservation of Linear Momentum](https://openstax.org/books/university-physics-volume-1/pages/9-3-conservation-of-linear-momentum) (<https://openstax.org/books/university-physics-volume-1/pages/9-3-conservation-of-linear-momentum>): Free textbook section.
- [OpenStax University Physics 1, 9.4 Types of Collisions](https://openstax.org/books/university-physics-volume-1/pages/9-4-types-of-collisions) (<https://openstax.org/books/university-physics-volume-1/pages/9-4-types-of-collisions>): Elastic and inelastic collisions.
- [OpenStax University Physics 1, 9.7 Rocket Propulsion](https://openstax.org/books/university-physics-volume-1/pages/9-7-rocket-propulsion) (<https://openstax.org/books/university-physics-volume-1/pages/9-7-rocket-propulsion>): Derivation of the rocket equation.
- [PhET: Collision Lab](https://phet.colorado.edu/en/simulations/collision-lab) (<https://phet.colorado.edu/en/simulations/collision-lab>): Elastic and inelastic collisions in 1D and 2D.



I finished this unit

Rotation, Torque & Angular Momentum

Everything that spins, from wheels and turbines to reaction wheels that point satellites, follows rotational versions of Newton's laws.

Learning objectives

By the end of this unit you can:

- Use angular position, velocity and acceleration, and link them to linear motion with $v = \omega r$.
- Compute moments of inertia and use $\tau = I\alpha$.
- Solve rolling problems with energy conservation.
- Apply conservation of angular momentum.

Key concepts

- Rotational quantities mirror linear ones: $\theta \leftrightarrow x$, $\omega \leftrightarrow v$, $\alpha \leftrightarrow a$, $I \leftrightarrow m$, $\tau \leftrightarrow F$, $L \leftrightarrow p$.
- Moment of inertia depends on how mass is spread from the axis. Mass far from the axis is harder to spin up.
- Torque is a force times its lever arm: $\tau = rF \sin \theta$.
- A rolling object has both translational and rotational kinetic energy, so it rolls down a slope slower than a frictionless block slides.
- With no external torque, angular momentum $L = I\omega$ stays constant.

Key equations

$$\omega = \frac{d\theta}{dt}, \quad \alpha = \frac{d\omega}{dt}, \quad v = \omega r$$

Angular velocity and acceleration

$$I = \sum m_i r_i^2, \quad I_{disk} = \frac{1}{2}MR^2$$

Moment of inertia

$$\tau = rF \sin \theta = I\alpha$$

Torque and Newton's second law for rotation

$$K_{rot} = \frac{1}{2}I\omega^2$$

Rotational kinetic energy

$$L = I\omega, \quad \tau_{\text{net}} = \frac{dL}{dt}$$

Angular momentum

Worked examples, step by step

Example 6.1 A wind-turbine rotor speeds up from rest to 1.5 rad/s in 30 s at a steady rate. Find α and how many turns it makes.

1. $\alpha = 1.5 \div 30 = 0.050 \text{ rad/s}^2$.
2. $\theta = \frac{1}{2}\alpha t^2 = \frac{1}{2} \times 0.050 \times 30^2 = 22.5 \text{ rad}$.
3. Turns: $22.5 \div 2\pi = 3.58$.

Answer: $\alpha = 0.050 \text{ rad/s}^2$; 3.58 turns.

Example 6.2 A solid ball rolls without slipping down a slope from 2.0 m high. How fast is it at the bottom?

1. For a solid sphere, $I = (2/5)mr^2$, and $\omega = v/r$.
2. $mgh = \frac{1}{2}mv^2 + \frac{1}{2}(2/5)mr^2(v/r)^2 = (7/10)mv^2$.
3. $v = \sqrt{(10gh/7)} = \sqrt{(10 \times 9.81 \times 2.0 \div 7)} = 5.29 \text{ m/s}$.

Answer: 5.29 m/s, less than the 6.26 m/s of a frictionless sliding block.

Example 6.3 A figure skater spinning at 2.0 rev/s pulls in her arms, cutting her moment of inertia from 4.0 to 1.6 kg·m². Find her new spin rate.

1. L is conserved: $I_1\omega_1 = I_2\omega_2$.
2. $\omega_2 = 4.0 \times 2.0 \div 1.6 = 5.0 \text{ rev/s}$.
3. Her kinetic energy rises by 2.5 times; the extra comes from the work her arms do.

Answer: 5.0 rev/s.

Practice problems

Work each on paper first, then check.

1. A 50 N force is applied at right angles to the end of a 0.30 m wrench. Find the torque.

$$\tau = 0.30 \times 50 = 15 \text{ N}\cdot\text{m}.$$

2. A child of 30 kg sits 2.0 m from a seesaw pivot. Where must a 40 kg child sit to balance?

$$30 \times 2.0 = 40 \times x, \text{ so } x = 1.5 \text{ m on the other side.}$$

3. A solid steel flywheel is a 100 kg disk of radius 0.50 m spinning at 300 rad/s. How much energy does it store?

$$I = \frac{1}{2} \times 100 \times 0.50^2 = 12.5 \text{ kg}\cdot\text{m}^2. K = \frac{1}{2} \times 12.5 \times 300^2 = 562,500 \text{ J} \approx 0.563 \text{ MJ (0.156 kWh)}.$$

4. A satellite has $I = 500 \text{ kg}\cdot\text{m}^2$ about one axis. An onboard reaction wheel with $I = 0.10 \text{ kg}\cdot\text{m}^2$ spins up from rest to 600 rad/s. How fast does the satellite turn?

$$\text{Total } L \text{ stays zero: } 0.10 \times 600 = 500 \times \omega, \text{ so } \omega = 0.12 \text{ rad/s the other way.}$$

5. A torque of 2.0 N·m acts on a disk with $I = 0.50 \text{ kg}\cdot\text{m}^2$. Find α .

$$\alpha = \tau/I = 4.0 \text{ rad/s}^2.$$

Common misconceptions

Myth: Torque depends only on the size of the force.

Actually: It also depends on where and at what angle you push. Pushing a door near the hinge barely turns it.

Myth: All round objects roll down a slope at the same speed.

Actually: A solid ball beats a solid cylinder, which beats a hoop. Less of their energy goes into spinning.

Myth: Pulling in your arms creates angular momentum.

Actually: Angular momentum stays the same; the spin rate rises because I falls.

Flashcards

Angular velocity ω

Rate of rotation, rad/s.

Moment of inertia I

Resistance to angular acceleration; $I = \sum mr^2$.

Torque τ

Turning effect of a force; $\tau = rF \sin \theta$ (N·m).

$$\tau = I\alpha$$

Newton's second law for rotation.

Angular momentum L

Rolling without slipping

$L = I\omega$; conserved with no external torque.

$v = \omega r$ at the contact point; total $K = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$.

Self-check quiz

1. Which reaches the bottom of a ramp first, rolling from rest? _____

A hoop

A solid disk

They tie

Whichever is heavier

A solid disk. The disk has the smaller $I/(mr^2)$, so more of its energy goes into forward motion.

2. The rotational analog of mass is... _____

torque

angular momentum

moment of inertia

angular velocity

moment of inertia. I resists angular acceleration just as m resists linear acceleration.

3. A satellite turns without firing thrusters by spinning a wheel inside it. This uses... _____

conservation of energy

conservation of angular momentum

Newton's first law only

gravity

conservation of angular momentum. Spinning the wheel one way turns the satellite the other way; total L stays constant.

4. Doubling the radius of a disk of the same mass multiplies I by...

2

4

$\frac{1}{2}$

8

4. $I = \frac{1}{2}MR^2$, so $2^2 = 4$.

Try this quiz again

How this helps save the planet

Reaction wheels are one common way spacecraft point their instruments: spinning a wheel one way turns the spacecraft the other way, as in the practice problem, without using propellant.

Wind turbines are rotational machines. The torque of the wind on the blades turns the rotor, and the generator converts that rotation into electricity.

Flywheels store energy as rotation and can smooth out the grid; the physics is exactly $K = \frac{1}{2}I\omega^2$.

On Saving Planets: [GRACE-FO](#) · [Earth observation](#)

Sources: [OpenStax University Physics 1, 11.3 Conservation of Angular Momentum](#) (<https://openstax.org/books/university-physics-volume-1/pages/11-3-conservation-of-angular-momentum>) · [U.S. DOE: How do wind turbines work?](#) (<https://www.energy.gov/eere/wind/how-do-wind-turbines-work>)

Free learning resources

- [OpenStax University Physics 1, 10.4 Moment of Inertia and Rotational Kinetic Energy](https://openstax.org/books/university-physics-volume-1/pages/10-4-moment-of-inertia-and-rotational-kinetic-energy) (<https://openstax.org/books/university-physics-volume-1/pages/10-4-moment-of-inertia-and-rotational-kinetic-energy>): Free textbook section.
- [OpenStax University Physics 1, 10.6 Torque](https://openstax.org/books/university-physics-volume-1/pages/10-6-torque) (<https://openstax.org/books/university-physics-volume-1/pages/10-6-torque>): Torque with examples.
- [PhET: Balancing Act](https://phet.colorado.edu/en/simulations/balancing-act) (<https://phet.colorado.edu/en/simulations/balancing-act>): Torque and balance on a seesaw.



I finished this unit

Gravitation & Orbits

Newton's law of gravity explains why satellites stay up, how long an orbit takes, and how to get from one orbit to another.

Learning objectives

By the end of this unit you can:

- Use Newton's law of universal gravitation and find g at any altitude.
- Find the speed and period of a circular orbit and the radius of a geostationary orbit.
- Use gravitational potential energy to find escape speed.
- Apply Kepler's three laws and estimate a Hohmann transfer.

Key concepts

- Every mass attracts every other mass with $F = Gm_1m_2/r^2$. Gravity weakens with the square of the distance from the center.
- A circular orbit happens when gravity supplies exactly the centripetal force: $GMm/r^2 = mv^2/r$.
- Kepler's laws: orbits are ellipses with the planet at one focus; a line to the planet sweeps equal areas in equal times; $T^2 \propto a^3$.
- Far from Earth, gravitational potential energy is $U = -GMm/r$. Escape speed is the speed that makes total energy zero.
- A Hohmann transfer moves between two circular orbits with two burns along a half-ellipse.

Key equations

$$F = \frac{Gm_1m_2}{r^2}, \quad g(r) = \frac{GM}{r^2}$$

Universal gravitation

$$v = \sqrt{\frac{GM}{r}}, \quad T = 2\pi\sqrt{\frac{r^3}{GM}}$$

Circular orbit speed and period

$$U = -\frac{GMm}{r}, \quad v_{esc} = \sqrt{\frac{2GM}{R}}$$

Potential energy and escape speed

$$T^2 = \frac{4\pi^2}{GM} a^3$$

Kepler's third law

Worked examples, step by step

Example 7.1 Find g at Earth's surface from G , Earth's mass and radius.

1. $g = GM/R^2 = 6.674 \times 10^{-11} \times 5.972 \times 10^{24} \div (6.371 \times 10^6)^2$.
2. $GM = 3.986 \times 10^{14} \text{ m}^3/\text{s}^2$; $R^2 = 4.059 \times 10^{13} \text{ m}^2$.
3. $g = 9.82 \text{ m/s}^2$.

Answer: 9.82 m/s^2 . Measured g varies from about 9.78 m/s^2 at the equator to 9.83 m/s^2 at the poles, because Earth spins and bulges at the equator; 9.81 m/s^2 is a convenient average.

Example 7.2 Landsat 9 orbits about 705 km above Earth. Treating the orbit as a circle, find its speed and period.

1. $r = 6,371 + 705 = 7,076 \text{ km} = 7.076 \times 10^6 \text{ m}$.
2. $v = \sqrt{GM/r} = \sqrt{(3.986 \times 10^{14} \div 7.076 \times 10^6)} = 7,505 \text{ m/s}$.
3. $T = 2\pi r/v = 2\pi \times 7.076 \times 10^6 \div 7,505 = 5,924 \text{ s} = 98.7 \text{ min}$.

Answer: 7.51 km/s and about 99 minutes per orbit, which matches the published figure.

Example 7.3 At what radius does a satellite orbit once per sidereal day (86,164 s), staying over one spot on the equator?

1. $r^3 = GM T^2/4\pi^2 = 3.986 \times 10^{14} \times 86,164^2 \div 39.48$.
2. $r^3 = 7.496 \times 10^{22}$.
3. $r = 4.216 \times 10^7 \text{ m} = 42,160 \text{ km}$ from Earth's center, about 35,790 km above the equator.

Answer: About 42,160 km from Earth's center: geostationary orbit, where many weather satellites sit.

Practice problems

Work each on paper first, then check.

1. Find the escape speed from Earth's surface.

$$v = \sqrt{(2GM/R)} = \sqrt{(2 \times 3.986 \times 10^{14} \div 6.371 \times 10^6)} = 11.2 \text{ km/s.}$$

2. At the ISS altitude of about 420 km, what fraction of surface gravity remains?

$$(6,371 \div 6,791)^2 = 0.880. \text{ Astronauts float because they are in free fall, not because gravity is gone.}$$

3. Mars orbits the Sun with a semi-major axis of 1.524 AU. How long is its year?

$$\text{Kepler: } T = a^{1.5} \text{ years} = 1.524^{1.5} = 1.88 \text{ Earth years.}$$

4. Estimate the total Δv for a Hohmann transfer from a 300 km circular orbit to geostationary radius (42,164 km).

$$r_1 = 6,671 \text{ km, } r_2 = 42,164 \text{ km. Burn 1: } \sqrt{(GM/r_1)}(\sqrt{(2r_2/(r_1 + r_2))} - 1) = 2.43 \text{ km/s. Burn 2: } \sqrt{(GM/r_2)}(1 - \sqrt{(2r_1/(r_1 + r_2))}) = 1.47 \text{ km/s. Total 3.90 km/s (plus any plane change).}$$

Common misconceptions

Myth: There is no gravity in orbit.

Actually: At 420 km, gravity is still 88% of its surface value. Astronauts and the station fall together.

Myth: A heavier satellite needs to go faster to stay in the same orbit.

Actually: $v = \sqrt{(GM/r)}$ has no satellite mass in it.

Myth: To catch up with a spacecraft ahead of you in the same orbit, speed up.

Actually: Speeding up raises your orbit and lengthens your period, so you fall behind. You slow down to drop into a faster, lower orbit.

Flashcards

Newton's law of gravitation

$$F = Gm_1m_2/r^2.$$

Orbital speed

$$v = \sqrt{(GM/r)} \text{ for a circle.}$$

Kepler's third law

$$T^2 \propto a^3.$$

Escape speed

$$v = \sqrt{(2GM/R)}; 11.2 \text{ km/s from Earth.}$$

Geostationary orbit

Period one sidereal day, about 35,790 km above the equator.

Hohmann transfer

Two-burn half-ellipse between circular orbits.

Self-check quiz

1. If you double your distance from Earth's center, gravity becomes...

$\frac{1}{2}$ as strong

$\frac{1}{4}$ as strong

2 times as strong

unchanged

$\frac{1}{4}$ as strong. Inverse square: $1/2^2 = 1/4$.

2. A lower circular orbit has a...

longer period and lower speed

shorter period and higher speed

longer period and higher speed

the same period

shorter period and higher speed. $v = \sqrt{GM/r}$ rises as r falls, and $T \propto r^{1.5}$ falls.

3. Kepler's second law means a planet moves fastest...

farthest from the Sun

closest to the Sun

at the same speed everywhere

only at the equinoxes

closest to the Sun. Equal areas in equal times: near the Sun the radius is short, so it must move faster.

4. Escape speed from Earth is about...

7.9 km/s

11.2 km/s

3.1 km/s

30 km/s

11.2 km/s. $\sqrt{(2GM/R)} = 11.2 \text{ km/s}$, $\sqrt{2}$ times the low-orbit speed.

Try this quiz again

How this helps save the planet

The twin GRACE-FO satellites fly about 220 km apart and measure the changing distance between them to about one micron. When the leading satellite passes over extra mass, such as a big aquifer or ice sheet, gravity tugs it ahead slightly. Mapping those tugs month by month shows where groundwater is being used up and how fast ice sheets are losing mass.

That gravity data helps people manage water during droughts and helps scientists track sea-level rise, which matters for coastal communities and wetlands alike.

Orbit choice is physics too: sun-synchronous orbits like Landsat 9's repeat lighting conditions so changes on the ground can be compared fairly, and geostationary orbits let weather satellites watch storms continuously.

On Saving Planets: [GRACE-FO](#) · [Orbital velocity calculator](#) · [Hohmann transfer calculator](#)

Sources: [NASA JPL: GRACE-FO \(https://gracefo.jpl.nasa.gov/\)](https://gracefo.jpl.nasa.gov/) · [NASA: Landsat 9 \(https://landsat.gsfc.nasa.gov/satellites/landsat-9/\)](https://landsat.gsfc.nasa.gov/satellites/landsat-9/)

Free learning resources

- [OpenStax University Physics 1, 13.4 Satellite Orbits and Energy \(https://openstax.org/books/university-physics-volume-1/pages/13-4-satellite-orbits-and-energy\)](https://openstax.org/books/university-physics-volume-1/pages/13-4-satellite-orbits-and-energy): Free textbook section.
- [OpenStax University Physics 1, 13.5 Kepler's Laws of Planetary Motion \(https://openstax.org/books/university-physics-volume-1/pages/13-5-keplers-laws-of-planetary-motion\)](https://openstax.org/books/university-physics-volume-1/pages/13-5-keplers-laws-of-planetary-motion): Kepler's laws derived and applied.
- [PhET: Gravity and Orbits \(https://phet.colorado.edu/en/simulations/gravity-and-orbits\)](https://phet.colorado.edu/en/simulations/gravity-and-orbits): Change masses and speeds and watch orbits form.
- [PhET: Kepler's Laws \(https://phet.colorado.edu/en/simulations/keplers-laws\)](https://phet.colorado.edu/en/simulations/keplers-laws): Explore all three laws.



I finished this unit

Oscillations & Introduction to Fluids

Springs and pendulums repeat in simple harmonic motion; fluids push with pressure and lift with buoyancy and flow.

Learning objectives

By the end of this unit you can:

- Describe simple harmonic motion and find period, frequency and maximum speed for a spring and a pendulum.
- Explain damping and resonance.
- Compute pressure at depth and buoyant force.
- Use the continuity equation and Bernoulli's equation for steady flow.

Key concepts

- A restoring force proportional to displacement ($F = -kx$) gives simple harmonic motion, $x = A \cos(\omega t + \phi)$.
- The period of a mass on a spring does not depend on amplitude; a pendulum's period depends only on its length and g for small swings.
- Pressure in a fluid increases with depth: $P = P_0 + \rho gh$.
- Archimedes: the buoyant force equals the weight of fluid pushed aside.
- In steady flow, a fluid speeds up where a pipe narrows (continuity), and faster flow has lower pressure (Bernoulli).

Key equations

$$x(t) = A \cos(\omega t + \phi)$$

Simple harmonic motion

$$\omega = \sqrt{\frac{k}{m}}, \quad T = 2\pi \sqrt{\frac{m}{k}}$$

Mass on a spring

$$T = 2\pi \sqrt{\frac{L}{g}}$$

Simple pendulum (small angles)

$$P = P_0 + \rho gh, \quad F_B = \rho_{\text{fluid}} V_{\text{sub}} g$$

Pressure at depth and buoyancy

$$A_1 v_1 = A_2 v_2, \quad P + \frac{1}{2} \rho v^2 + \rho gh = \text{const}$$

Continuity and Bernoulli

Worked examples, step by step

Example 8.1 A 0.50 kg mass on a spring with $k = 200 \text{ N/m}$ is pulled 5.0 cm and released. Find ω , the period, the frequency and the maximum speed.

1. $\omega = \sqrt{k/m} = \sqrt{200 \div 0.50} = 20 \text{ rad/s}$.
2. $T = 2\pi/\omega = 0.314 \text{ s}$; $f = 1/T = 3.18 \text{ Hz}$.
3. $v_{\text{max}} = A\omega = 0.050 \times 20 = 1.0 \text{ m/s}$.

Answer: $\omega = 20 \text{ rad/s}$, $T = 0.314 \text{ s}$, $f = 3.18 \text{ Hz}$, $v_{\text{max}} = 1.0 \text{ m/s}$.

Example 8.2 What is the period of a 1.00 m pendulum on Earth, and on the Moon ($g = 1.62 \text{ m/s}^2$)?

1. Earth: $T = 2\pi\sqrt{1.00 \div 9.81} = 2.01 \text{ s}$.
2. Moon: $T = 2\pi\sqrt{1.00 \div 1.62} = 4.94 \text{ s}$.

Answer: 2.01 s on Earth, 4.94 s on the Moon.

Example 8.3 Water flows at 2.0 m/s through a level pipe 4.0 cm across, which narrows to 2.0 cm. Find the new speed and the pressure drop.

1. Area falls by $(2.0/4.0)^2 = 1/4$, so $v_2 = 4 \times 2.0 = 8.0 \text{ m/s}$.
2. Bernoulli, level pipe: $\Delta P = \frac{1}{2}\rho(v_2^2 - v_1^2) = \frac{1}{2} \times 1,000 \times (64 - 4.0) = 30,000 \text{ Pa}$.

Answer: 8.0 m/s and a pressure drop of 30 kPa.

Practice problems

Work each on paper first, then check.

1. What is the extra pressure 10 m below the surface of seawater ($\rho = 1,025 \text{ kg/m}^3$)?

$pgh = 1,025 \times 9.81 \times 10 = 100,600 \text{ Pa}$, about one more atmosphere.

2. A block of wood with density 600 kg/m^3 floats in fresh water. What fraction is under water?

Floating: $\rho_{\text{wood}} V g = \rho_{\text{water}} V_{\text{sub}} g$, so $V_{\text{sub}}/V = 600/1,000 = 0.60$.

3. A pendulum must have a period of exactly 2.00 s. How long should it be?

$L = g(T/2\pi)^2 = 9.81 \times (2.00 \div 6.283)^2 = 0.994 \text{ m}$.

4. Why can soldiers be told to break step when crossing a bridge?

Marching in step pushes the bridge at a steady frequency. If that matches a natural frequency of the bridge, resonance can build up large oscillations.

Common misconceptions

Myth: A bigger swing makes a pendulum take longer.

Actually: For small swings the period does not depend on amplitude, only on L and g .

Myth: Heavy things sink and light things float.

Actually: Density decides. A steel ship floats because its shape pushes aside a weight of water equal to its own weight.

Myth: Faster-flowing fluid has higher pressure.

Actually: In steady, level flow, faster flow has lower pressure (Bernoulli).

Flashcards

Simple harmonic motion

Oscillation with restoring force $\propto$ displacement;

$x = A \cos(\omega t + \phi)$.

Period

Time for one cycle; $T = 1/f$.

Resonance

Large response when driven at a natural frequency.

Pressure

Force per area, $P = F/A$ (Pa).

Archimedes' principle

Buoyant force = weight of displaced fluid.

Bernoulli's equation

$P + \frac{1}{2}\rho v^2 + \rho gh$ is constant along a streamline in steady, ideal flow.

Self-check quiz

1. Quadrupling the mass on a spring changes the period by a factor of... _____

4

2

$\frac{1}{2}$

$\frac{1}{4}$

2. $T \propto \sqrt{m}$, and $\sqrt{4} = 2$.

2. The buoyant force on a submerged object equals... _____

its own weight

the weight of fluid it displaces

the fluid pressure

zero

the weight of fluid it displaces. Archimedes' principle.

3. Water speeds up where a hose narrows because of... _____

continuity ($A_1v_1 = A_2v_2$)

buoyancy

resonance

friction

continuity ($A_1v_1 = A_2v_2$). The same volume per second must pass through a smaller area.

4. A pendulum clock is taken to the Moon. It runs... _____

faster

slower

the same

backward

slower. Lower g gives a longer period, so it ticks less often.

Try this quiz again

How this helps save the planet

Lift on a wing and on a wind-turbine blade comes from the air flowing faster over one side, which lowers the pressure there. Bernoulli's equation is the first step in designing blades and wings that waste less energy.

Oscillation physics matters for clean-energy machines too: any tall structure that is pushed rhythmically, as a turbine tower is by its spinning rotor, can build up large vibrations if the push matches one of its natural frequencies (resonance).

Fluid pressure and buoyancy are behind ocean science too, from floats that measure the deep ocean to satellites such as Sentinel-6 that measure sea level to help coastal communities plan.

On Saving Planets: [Pendulum period calculator](#) · [Lift equation calculator](#) · [Sentinel-6B](#)

Sources: U.S. DOE: How do wind turbines work? (<https://www.energy.gov/eere/wind/how-do-wind-turbines-work>) · NASA: Sentinel-6 sea level mission (<https://sealevel.nasa.gov/missions/sentinel-6>)

Free learning resources

- [OpenStax University Physics 1, 15.1 Simple Harmonic Motion](https://openstax.org/books/university-physics-volume-1/pages/15-1-simple-harmonic-motion) (<https://openstax.org/books/university-physics-volume-1/pages/15-1-simple-harmonic-motion>): Free textbook section.
- [OpenStax University Physics 1, 15.4 Pendulums](https://openstax.org/books/university-physics-volume-1/pages/15-4-pendulums) (<https://openstax.org/books/university-physics-volume-1/pages/15-4-pendulums>): Simple and physical pendulums.
- [OpenStax University Physics 1, 14.4 Archimedes' Principle and Buoyancy](https://openstax.org/books/university-physics-volume-1/pages/14-4-archimedes-principle-and-buoyancy) (<https://openstax.org/books/university-physics-volume-1/pages/14-4-archimedes-principle-and-buoyancy>): Buoyancy with examples.
- [OpenStax University Physics 1, 14.6 Bernoulli's Equation](https://openstax.org/books/university-physics-volume-1/pages/14-6-bernoullis-equation) (<https://openstax.org/books/university-physics-volume-1/pages/14-6-bernoullis-equation>): Flow, pressure and lift.
- [PhET: Pendulum Lab](https://phet.colorado.edu/en/simulations/pendulum-lab) (<https://phet.colorado.edu/en/simulations/pendulum-lab>): Period, length, mass and gravity.
- [PhET: Masses and Springs](https://phet.colorado.edu/en/simulations/masses-and-springs) (<https://phet.colorado.edu/en/simulations/masses-and-springs>): Springs, energy and damping.

- [PhET: Buoyancy](https://phet.colorado.edu/en/simulations/buoyancy) (<https://phet.colorado.edu/en/simulations/buoyancy>): Density and buoyant force.
- [PhET: Under Pressure](https://phet.colorado.edu/en/simulations/under-pressure) (<https://phet.colorado.edu/en/simulations/under-pressure>): Pressure at depth.



I finished this unit

The lab (PHYS 110L)

The lab is the hands-on part of the course, a 1-credit component in a typical college schedule. Here it is free and for practice only.

Each lab tests one idea from lecture against real measurements, and each one asks you to state an uncertainty. A result without an uncertainty cannot be compared with a prediction. Every lab also has a home or PhET version.

Safety reference: [OSHA: workplace safety](https://www.osha.gov/) (<https://www.osha.gov/>)

Lab A: Measurement and uncertainty (measuring g)

WEEK 1

Goal: Time a ball dropped from a measured height, find g, and state a proper uncertainty.

$$g = \frac{2h}{t^2}, \quad \frac{\delta g}{g} = \sqrt{\left(\frac{\delta h}{h}\right)^2 + \left(2\frac{\delta t}{t}\right)^2}$$

Propagate relative uncertainties in quadrature; time is squared, so its relative uncertainty counts twice

Procedure

1. Measure the drop height h from the bottom of the ball to the floor; estimate δh (for a tape, about ± 2 mm).
2. Drop a dense ball from rest and time the fall. A phone slow-motion video or a sound-trigger app beats a hand stopwatch.
3. Repeat at least five times.
4. Find the mean time, the sample standard deviation s and the standard error $s/\sqrt{N}$; use the standard error as δt .
5. Compute g and δg , and compare with 9.81 m/s^2 .

Data table

Trial	Fall time (s)
1	0.55
2	0.56
3	0.54
4	0.55
5	0.56
Mean	0.552
Std. deviation s	0.0084
Standard error $s/\sqrt{5}$	0.0037

Sample data for practice only. $h = 1.500 \pm 0.002 \text{ m}$.

Sample calculation

1. $g = 2h/t^2 = 2 \times 1.500 \div 0.552^2 = 9.85 \text{ m/s}^2$.
2. Relative uncertainty from time: $2 \times 0.0037 \div 0.552 = 1.36\%$. From height: $0.002 \div 1.500 = 0.13\%$.

3. Combined: $\sqrt{(1.36^2 + 0.13^2)} = 1.36\%$, so $\delta g = 0.0136 \times 9.85 = 0.13 \text{ m/s}^2$.

4. Result: $g = 9.85 \pm 0.13 \text{ m/s}^2$. The accepted 9.81 m/s^2 lies inside the range, so the two agree.

Timing dominates the uncertainty.

Safety

- Drop the ball only where nobody is underneath, and keep the floor clear.
- Stand on a sturdy surface, not a chair, to reach the release height.

Home or virtual alternative

- Do it exactly as written at home with a phone slow-motion video.
- Or use the PhET Projectile Motion sim with launch speed 0 to check timing.

PhET: Projectile Motion (<https://phet.colorado.edu/en/simulations/projectile-motion>) · JCGM uncertainty guide (GUM) (<https://www.bipm.org/en/committees/jc/jcgm/publications>)

Planet link: GRACE-FO's science only works because its team knows the uncertainty of every distance it measures; a change counts only when it beats that uncertainty. [NASA JPL: GRACE-FO \(https://gracefo.jpl.nasa.gov/\)](https://gracefo.jpl.nasa.gov/)



I completed this lab (wet or virtual)

Lab B: Projectile motion

WEEK 3

Goal: Measure a launcher's speed from a horizontal shot, then predict and test where an angled shot lands.

$$v_0 = \frac{x}{\sqrt{2h/g}}, \quad R = \frac{v_0^2 \sin 2\theta}{g}$$

Launch speed from a horizontal shot, then the predicted range

Procedure

1. Fire a ball horizontally from a launcher (or roll it off a ramp) at table height h .
2. Tape carbon paper over plain paper where it lands; do five shots and measure each landing distance x .
3. Find the mean x and compute v_0 .
4. Predict the range for a 30° launch from floor level, mark the spot, and test it with five shots.
5. Compare prediction and result; list sources of error (air drag, launch height, angle reading).

Data table

Quantity	Value
Table height h	1.00 m
Mean landing distance x	2.26 m
Fall time $\sqrt{2h/g}$	0.452 s
Launch speed v_0	5.01 m/s
Predicted range at 30°	2.21 m

Sample data for practice only.

Sample calculation

1. $t = \sqrt{2 \times 1.00 \div 9.81} = 0.452$ s.
2. $v_0 = 2.26 \div 0.452 = 5.01$ m/s.
3. $R(30^\circ) = 5.01^2 \times \sin 60^\circ \div 9.81 = 25.1 \times 0.866 \div 9.81 = 2.21$ m.
4. Percent difference = $|\text{measured} - \text{predicted}| \div \text{predicted} \times 100\%$.

Safety

- Wear eye protection with any spring launcher, and never aim it at a person.

- Keep the landing zone clear.

Home or virtual alternative

- Roll a marble off a table and measure x ; skip the angled part or use the PhET sim for it.

PhET: Projectile Motion (<https://phet.colorado.edu/en/simulations/projectile-motion>)

Planet link: The same prediction-then-test method is used to forecast where a reentering rocket stage could land.



I completed this lab (wet or virtual)

Lab C: Newton's second law

WEEK 5

Goal: Show that acceleration is proportional to net force and inversely proportional to mass.

$$a = \frac{m_h g}{m_c + m_h}$$

Cart pulled by a hanging mass over a pulley, ignoring friction

Procedure

1. Level a track. Attach a cart (mass m_c) by string over a pulley to a hanging mass m_h .
2. Release from rest and record the motion with a sensor, video or by timing a known distance ($a = 2d/t^2$).
3. Repeat for five hanging masses, moving mass from the cart to the hanger so the total stays fixed.
4. Graph a against $m_h g$. The slope should be $1/(m_c + m_h)$.
5. Repeat with extra mass on the cart to test the mass dependence.

Data table

Quantity	Value
Cart mass m_c	0.500 kg
Hanging mass m_h	0.050 kg
Predicted a	0.892 m/s ²
Measured a	0.86 m/s ²

Sample data for practice only.

Sample calculation

1. Predicted $a = 0.050 \times 9.81 \div 0.550 = 0.892 \text{ m/s}^2$.
2. Measured 0.86 m/s^2 is 3.6% lower.
3. Friction force needed to explain the gap: $(0.892 - 0.86) \times 0.550 = 0.018 \text{ N}$, a reasonable rolling friction.

Safety

- Put a soft stop at the end of the track and keep fingers clear of the pulley.

Home or virtual alternative

- Use PhET Forces and Motion: Basics (Acceleration screen) to vary force and mass.

PhET: Forces and Motion: Basics (<https://phet.colorado.edu/en/simulations/forces-and-motion-basics>)

Planet link: $F = ma$ is why lighter vehicles need less energy to speed up: every kilogram saved cuts the force, and the fuel, needed.



I completed this lab (wet or virtual)

Lab D: Friction

WEEK 5

Goal: Measure static and kinetic friction coefficients with a tilting ramp.

$$\mu_s = \tan \theta_{\text{slip}}, \quad \mu_k = \tan \theta_{\text{steady}}$$

On a ramp, friction balances $mg \sin \theta$ when $N = mg \cos \theta$

Procedure

1. Place a block on a board and slowly raise one end until the block just starts to slide; record the angle θ_{slip} . Repeat five times.
2. Find the angle at which the block, given a tap, slides down at a steady speed: θ_{steady} .
3. Compute μ_s and μ_k . Repeat on a second surface (felt, rubber).

Data table

Quantity	Value
Block mass	0.250 kg
Mean slip angle	31°
Mean steady-slide angle	24°
μ_s	0.60
μ_k	0.45

Sample data for practice only.

Sample calculation

1. $\mu_s = \tan 31^\circ = 0.601$.
2. $\mu_k = \tan 24^\circ = 0.445$.
3. As expected, $\mu_k < \mu_s$. The mass does not appear: it cancels.

Safety

- Keep the ramp low and stable; catch the block at the bottom.

Home or virtual alternative

- A book, a phone inclinometer app and a hardcover board work fine.
- PhET The Ramp lets you set friction and watch the forces.

PhET: The Ramp (<https://phet.colorado.edu/en/simulations/the-ramp>)

Planet link: Rolling friction in tires is one of the forces a vehicle burns energy against at every speed; lower-friction designs save fuel. U.S. DOE: Vehicle Technologies Office (<https://www.energy.gov/eere/vehicles/vehicle-technologies-office>)



I completed this lab (wet or virtual)

Lab E: Conservation of energy

WEEK 7

Goal: Compare a cart's measured speed at the bottom of a ramp with the speed energy conservation predicts.

$$v = \sqrt{2gh}, \quad \text{fraction kept} = \frac{v_{meas}^2}{2gh}$$

Ideal speed from a drop h , and how much mechanical energy survived

Procedure

1. Measure the vertical drop h of a ramp.
2. Release a low-friction cart from rest and measure its speed at the bottom (photogate, or video over a short known distance).
3. Repeat five times and average.
4. Compute the predicted speed and the fraction of energy kept; explain where the rest went.

Data table

Quantity	Value
Drop height h	0.300 m
Predicted speed	2.43 m/s
Measured speed (mean)	2.35 m/s
Energy kept	93.8%

Sample data for practice only.

Sample calculation

1. $v = \sqrt{2 \times 9.81 \times 0.300} = 2.43 \text{ m/s}$.
2. Fraction kept = $2.35^2 \div (2 \times 9.81 \times 0.300) = 5.52 \div 5.89 = 0.938$.
3. About 6.2% of the mechanical energy became heat and sound through friction and drag.

Safety

- Clamp the ramp and stop the cart at the bottom.

Home or virtual alternative

- Roll a ball down a book-ramp and time it over a measured flat run.

- PhET Energy Skate Park shows the same energy bar charts.

PhET: Energy Skate Park (<https://phet.colorado.edu/en/simulations/energy-skate-park>)

Planet link: Tracking where energy goes is how engineers find savings, from regenerative braking to pumped-storage hydro. [U.S. DOE: Electric vehicle basics \(https://afdc.energy.gov/vehicles/electric-basics-ev\)](https://afdc.energy.gov/vehicles/electric-basics-ev)



I completed this lab (wet or virtual)

Lab F: Momentum and collisions

WEEK 8

Goal: Test conservation of momentum in elastic and sticky collisions, and measure how much kinetic energy is lost.

$$m_1v_1 + m_2v_2 = (m_1 + m_2)v_f$$

Perfectly inelastic collision

Procedure

1. On a level track, send cart 1 into cart 2 at rest with Velcro facing so they stick.
2. Measure speeds just before and after (sensor or video).
3. Repeat with magnets or springs facing for a nearly elastic bounce.
4. For each run, compare total momentum and total kinetic energy before and after.

Data table

Quantity	Value
$m_1 = m_2$	0.50 kg
v_1 before	0.80 m/s
Predicted v after (stuck)	0.40 m/s
Measured v after	0.39 m/s

Sample data for practice only.

Sample calculation

1. p before = $0.50 \times 0.80 = 0.40 \text{ kg}\cdot\text{m/s}$. p after = $1.00 \times 0.39 = 0.39 \text{ kg}\cdot\text{m/s}$, a 2.5% difference (friction during the run).
2. K before = $\frac{1}{2} \times 0.50 \times 0.80^2 = 0.160 \text{ J}$. K after = $\frac{1}{2} \times 1.00 \times 0.39^2 = 0.076 \text{ J}$.
3. About half the kinetic energy was lost, as theory predicts for equal masses sticking (exactly 50% ideally).

Safety

- Keep speeds low and stop carts before the track ends.

Home or virtual alternative

- PhET Collision Lab lets you set elasticity from 0% to 100%.

PhET: Collision Lab (<https://phet.colorado.edu/en/simulations/collision-lab>)

Planet link: DART used exactly this physics on an asteroid: a planned, measured collision to change a moonlet's orbit. NASA: DART mission (<https://science.nasa.gov/mission/dart/>)



I completed this lab (wet or virtual)

Lab G: Rotational inertia

WEEK 10

Goal: Measure a disk's moment of inertia with a falling mass and compare it with $\frac{1}{2}MR^2$.

$$I = mr^2 \left(\frac{g}{a} - 1 \right), \quad a = \frac{2d}{t^2}$$

Hanging mass m on a string wound around an axle of radius r

Procedure

1. Wind a string around the disk's axle (radius r) and hang a mass m from it.
2. Release from rest and time the fall through a height d ; repeat five times.
3. Compute a , then I . Measure the disk's mass M and radius R and compute $\frac{1}{2}MR^2$.
4. Compare. Then add a ring and see how much I grows.

Data table

Quantity	Value
Hanging mass m	0.050 kg
Axle radius r	0.025 m
Fall distance d	0.800 m
Mean fall time t	4.00 s
Disk M, R	1.50 kg, 0.064 m

Sample data for practice only.

Sample calculation

1. $a = 2 \times 0.800 \div 4.00^2 = 0.100 \text{ m/s}^2$.
2. $I = 0.050 \times 0.025^2 \times (9.81 \div 0.100 - 1) = 0.050 \times 0.000625 \times 97.1 = 3.03 \times 10^{-3} \text{ kg}\cdot\text{m}^2$.
3. $\frac{1}{2}MR^2 = \frac{1}{2} \times 1.50 \times 0.064^2 = 3.07 \times 10^{-3} \text{ kg}\cdot\text{m}^2$.
4. Difference 1.2%, within the uncertainty of the radius and timing.

Safety

- Keep the hanging mass low over a soft landing pad.

Home or virtual alternative

- Roll a full can of soup and an empty can down the same ramp and compare times; explain the result with $K = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$.

OpenStax 10.4 Moment of Inertia (<https://openstax.org/books/university-physics-volume-1/pages/10-4-moment-of-inertia-and-rotational-kinetic-energy>)

Planet link: Reaction wheels that point Earth-observing satellites are designed around exactly this quantity.



I completed this lab (wet or virtual)

Lab H: Pendulum and simple harmonic motion

WEEK 13

Goal: Test $T = 2\pi\sqrt{L/g}$, show the period does not depend on mass or small amplitude, and measure g a second way.

$$g = \frac{4\pi^2 L}{T^2}$$

Rearranged pendulum equation

Procedure

1. Hang a dense bob on a string; measure L from the pivot to the bob's center.
2. Pull it back less than 10° and time 20 full swings; divide by 20 for T .
3. Repeat for five lengths. Graph T^2 against L : the slope is $4\pi^2/g$.
4. Change the bob mass and the amplitude (still small) and check that T stays the same.
5. Optional: time a mass bouncing on a spring and test $T = 2\pi\sqrt{m/k}$.

Data table

Quantity	Value
Length L	0.800 m
Time for 20 swings	35.9 s
Period T	1.795 s
g	9.80 m/s ²

Sample data for practice only.

Sample calculation

1. $T = 35.9 \div 20 = 1.795$ s. Timing 20 swings divides the reaction-time error by 20.
2. $g = 4\pi^2 \times 0.800 \div 1.795^2 = 31.58 \div 3.222 = 9.80$ m/s².
3. Compare with Lab A: two independent methods, and the pendulum is far more precise.

Safety

- Use a secure pivot and swing the bob away from faces.

Home or virtual alternative

- A key on a shoelace works; time it with a phone.

PhET: Pendulum Lab (<https://phet.colorado.edu/en/simulations/pendulum-lab>) · PhET: Masses and Springs (<https://phet.colorado.edu/en/simulations/masses-and-springs>)

Planet link: Precise knowledge of g , and of its tiny changes from place to place, is what gravity missions such as GRACE-FO turn into maps of water and ice. [NASA JPL: GRACE-FO \(https://gracefo.jpl.nasa.gov/\)](https://gracefo.jpl.nasa.gov/)

☐ I completed this lab (wet or virtual)

Exam prep practice sets

Time yourself: about 10 minutes per problem. Then compare with the full solutions.

Midterm practice set (Units 1–4)

1. A rocket accelerates straight up from rest at 5.0 m/s^2 for 20 s, then its engine stops. What is the maximum height it reaches?

1. At burnout: $v = 5.0 \times 20 = 100 \text{ m/s}$; height = $\frac{1}{2} \times 5.0 \times 20^2 = 1,000 \text{ m}$.
2. Coasting up: extra height = $v^2/2g = 100^2 \div 19.62 = 510 \text{ m}$.

Answer: 1,510 m, ignoring drag.

2. A ball is kicked at 25 m/s at 40° above level ground. Find its range and time of flight.

1. $v_y = 25 \sin 40^\circ = 16.1 \text{ m/s}$; $t = 2 \times 16.1 \div 9.81 = 3.28 \text{ s}$.
2. $R = 25^2 \times \sin 80^\circ \div 9.81 = 625 \times 0.985 \div 9.81 = 62.7 \text{ m}$.

Answer: 62.7 m in 3.28 s.

3. A 20 kg sled is pulled at constant speed across snow ($\mu_k = 0.10$) by a horizontal rope. Find the rope tension and the work done over 50 m.

1. Constant speed: $T = \mu_k mg = 0.10 \times 20 \times 9.81 = 19.6 \text{ N}$.
2. $W = 19.6 \times 50 = 981 \text{ J}$.

Answer: 19.6 N; 981 J, all turned into heat by friction.

4. A 2.0 kg block slides from rest down a frictionless curved track from 5.0 m high and then compresses a spring ($k = 400 \text{ N/m}$) on level ground. Find the maximum compression.

1. $mgh = \frac{1}{2}kx^2$.
2. $x = \sqrt{(2 \times 2.0 \times 9.81 \times 5.0 \div 400)} = \sqrt{0.4905} = 0.700 \text{ m}$.

Answer: 0.700 m.

Final practice set (all units)

1. A 3.0 kg cart at 4.0 m/s collides with a 1.0 kg cart at rest and they stick. Find the final speed and the fraction of kinetic energy lost.

1. $v = 3.0 \times 4.0 \div 4.0 = 3.0 \text{ m/s}$.

2. $K \text{ before} = 24 \text{ J}$; $\text{after} = \frac{1}{2} \times 4.0 \times 9.0 = 18 \text{ J}$.

Answer: 3.0 m/s; 25% of the kinetic energy is lost.

2. A hollow ring and a solid disk of equal mass and radius roll from rest down a ramp 1.0 m high. Find each speed at the bottom.

1. Ring ($I = mr^2$): $mgh = mv^2$, so $v = \sqrt{gh} = 3.13 \text{ m/s}$.

2. Disk ($I = \frac{1}{2}mr^2$): $mgh = \frac{3}{4}mv^2$, so $v = \sqrt{(4gh/3)} = 3.62 \text{ m/s}$.

Answer: Ring 3.13 m/s, disk 3.62 m/s; the disk wins.

3. Find the orbital period of a satellite in a circular orbit 1,336 km above Earth.

1. $r = 6,371 + 1,336 = 7,707 \text{ km}$.

2. $T = 2\pi\sqrt{(r^3/GM)} = 2\pi\sqrt{((7.707 \times 10^6)^3 \div 3.986 \times 10^{14})} = 6,733 \text{ s}$.

Answer: About 112 minutes.

4. A 0.20 kg mass on a spring oscillates with a period of 0.50 s and amplitude 0.10 m. Find k and the maximum speed.

1. $\omega = 2\pi \div 0.50 = 12.57 \text{ rad/s}$.

2. $k = m\omega^2 = 0.20 \times 158.0 = 31.6 \text{ N/m}$.

3. $v_{\text{max}} = A\omega = 0.10 \times 12.57 = 1.26 \text{ m/s}$.

Answer: $k = 31.6 \text{ N/m}$; $v_{\text{max}} = 1.26 \text{ m/s}$.

5. A 1.0 m^3 buoy of mass 400 kg is held fully under seawater ($\rho = 1,025 \text{ kg/m}^3$) by a cable to the seabed. Find the cable tension.

1. Buoyant force $= 1,025 \times 1.0 \times 9.81 = 10,060 \text{ N}$.

2. Weight $= 400 \times 9.81 = 3,920 \text{ N}$.

3. Tension $= 10,060 - 3,920 = 6,130 \text{ N}$.

Answer: About 6,130 N.

Formula sheet

$$v = dx/dt, \quad a = dv/dt$$

$$x = x_0 + v_0t + \frac{1}{2}at^2$$

$$v^2 = v_0^2 + 2a\Delta x$$

$$R = v_0^2 \sin 2\theta / g$$

$$a_c = v^2 / r = \omega^2 r$$

$$\sum F_i = ma_i$$

$$fk = \mu_k N$$

$$W = \int F_i \cdot dx_i$$

$$K = \frac{1}{2}mv^2, U_g = mgh, U_s = \frac{1}{2}kx^2$$

$$P = dW/dt = Fv$$

$$p_i = mv_i, J = \Delta p_i$$

$$\Delta v = v_e \ln(m_0/m_f)$$

$$\tau = rF \sin \theta = I\alpha$$

$$L = I\omega, K_{rot} = \frac{1}{2}I\omega^2$$

$$F = Gm_1m_2/r^2$$

$$v_{orb} = \sqrt{GM/r}, v_{esc} = \sqrt{2GM/R}$$

$$T^2 = 4\pi^2 a^3 / GM$$

$$T_{spring} = 2\pi\sqrt{m/k}, T_{pend} = 2\pi\sqrt{L/g}$$

$$P = P_0 + \rho gh, F_B = \rho Vg$$

$$A_1v_1 = A_2v_2, P + \frac{1}{2}\rho v^2 + \rho gh = \text{const}$$

Constants

Constant	Value
Gravitational constant, G	$6.674 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2$
Standard gravity, g	9.81 m/s ² (9.80665 m/s ² by definition)
Mass of Earth	$5.972 \times 10^{24} \text{ kg}$ (NASA Earth fact sheet)
Mean radius of Earth	6,371 km (NASA Earth fact sheet)
GM of Earth	$3.986 \times 10^{14} \text{ m}^3/\text{s}^2$
Sidereal day	86,164 s
Density of fresh water	1,000 kg/m ³ ; seawater about 1,025 kg/m ³
Density of air at sea level, 15 °C	1.225 kg/m ³

Reference data

Use these free, official data sources alongside the course.

- [NASA Earth fact sheet \(https://nssdc.gsfc.nasa.gov/planetary/factsheet/earthfact.html\)](https://nssdc.gsfc.nasa.gov/planetary/factsheet/earthfact.html): Mass, radius, gravity and orbit data for Earth (and links to other planets).
- [NIST SI units \(https://www.nist.gov/pml/owm/metric-si/si-units\)](https://www.nist.gov/pml/owm/metric-si/si-units): The seven SI base units and how they are defined.
- [JCGM publications \(GUM\) \(https://www.bipm.org/en/committees/jc/jcgm/publications\)](https://www.bipm.org/en/committees/jc/jcgm/publications): The international guide to expressing measurement uncertainty.

Glossary

Acceleration

Rate of change of velocity, dv/dt .

Amplitude

Maximum displacement from equilibrium in an oscillation.

Angular momentum

$L = I\omega$; conserved without external torque.

Buoyant force

Upward force from a fluid, equal to the weight of fluid displaced.

Center of mass

Mass-weighted average position of a system.

Conservative force

A force whose work does not depend on path, such as gravity or a spring.

Displacement

Change in position, a vector.

Elastic collision

A collision that conserves kinetic energy.

Escape speed

Minimum speed to leave a body's gravity without further thrust.

Free-body diagram

Diagram of all forces on one object.

Frequency

Cycles per second (Hz); $f = 1/T$.

Geostationary orbit

An equatorial orbit with a one-sidereal-day period.

Impulse

Force integrated over time; equals change in momentum.

Inertia

Resistance to change in motion; measured by mass.

Kinetic energy

Energy of motion, $\frac{1}{2}mv^2$.

Moment of inertia

Rotational inertia, Σmr^2 .

Momentum

$p = mv$.

Newton

SI unit of force, $\text{kg}\cdot\text{m}/\text{s}^2$.

Period

Time for one cycle or one orbit.

Power

Rate of energy transfer, in watts.

Pressure

Force per unit area, in pascals.

Resonance

Large oscillation when driven at a natural frequency.

Standard error

Standard deviation of the mean, $s/\sqrt{N}$.

Sun-synchronous orbit

A near-polar orbit that passes over each place at about the same local solar time.

Torque

Turning effect of a force, $rF \sin \theta$.

Uncertainty

Estimated range around a measured value that probably contains the true value.

Vector

A quantity with size and direction.

Weight

Gravitational force on a mass, mg .

Work

Energy transferred by a force over a displacement.

Self-assessment rubric

No grade or credit is given. Use this to judge honestly where you are in each unit.

Level	What it looks like
4 · Mastery	Solves new, unseen problems correctly, starts from a diagram and a principle (Newton, energy or momentum), and checks units and limits.
3 · Proficient	Solves the practice problems with correct units and sensible significant figures; occasional slips.
2 · Developing	Follows worked examples but struggles to choose a method for new problems, or mixes up vectors and scalars.
1 · Beginning	Plugs numbers into formulas without a diagram; needs to revisit the unit.

Suggested weighting if you want a score

Part	Weight
Practice problems	30%
Lab write-ups (or virtual labs)	20%
Midterm practice set	20%
Final practice set	30%

Aim for level 3 or better in every unit before moving to the next course.